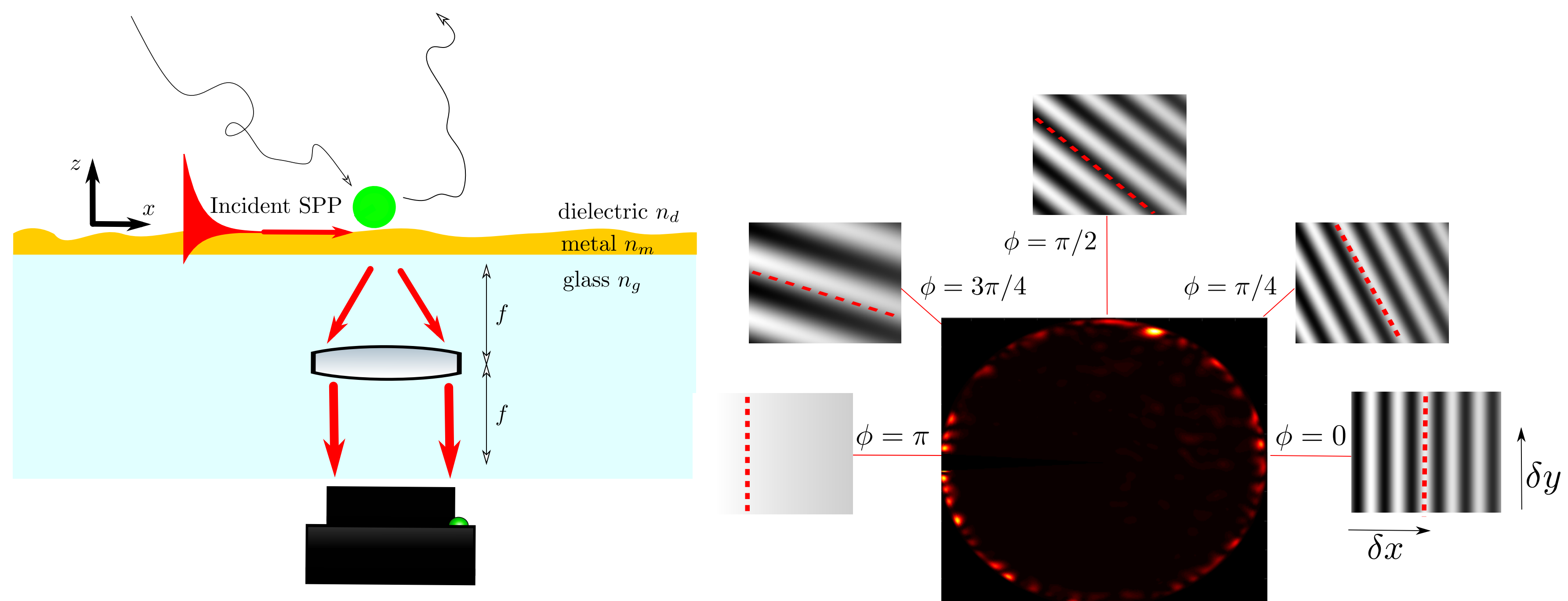


## MOTIVATION

- **Detection and tracking of single nanometre scale biological molecules:** small particles interact only weakly with light
- **Enhance light-matter interaction using plasmonics:** confined surface modes give strong local fields<sup>1</sup>
- **Interference with strong background field to increase sensitivity:** Interferometric signals are sensitive to small phase perturbations<sup>2</sup>

## Principle

- ▶ **Scattered light strongly confined to cone:** due to conservation of SPP momentum<sup>3</sup>
- ▶ **Random scattering by rough surface:** random interference of wavefronts gives speckle pattern
- ▶ **Light scattered by analyte particle has known phase (and amplitude) dependence on particle position:** fringe patterns at different directions,  $\phi$ , on the cone as the analyte particle moves (assuming single scattering)
- ▶ **Random speckle phase:** unknown random offsets of fringe pattern, different for each  $\phi$
- ▶ **Eliminate unknown phase using 3 frames in particle trajectory**
- ▶ **Solve simultaneously the N equations for N pixels around the ring for analyte particle displacement between frames**



	Performance Metric	Shot Noise limit	'Dark' limit	Noise
Dark Field	SNR = dSNR	$\sqrt{N_s}$	$N_s/\sqrt{N_d} \ll 1$	
	SBR	$N_s/N_d \gg 1$	$N_s/N_d \ll 1$	
Interference	SNR	$\sqrt{N_b} \gg 1$	$\sqrt{N_b} \gg 1$	
	SBR	$\sqrt{N_s/N_b} \ll 1$	$\sqrt{N_s/N_b} \ll 1$	
	dSNR	$\sqrt{N_s}$	$\sqrt{N_s}$	

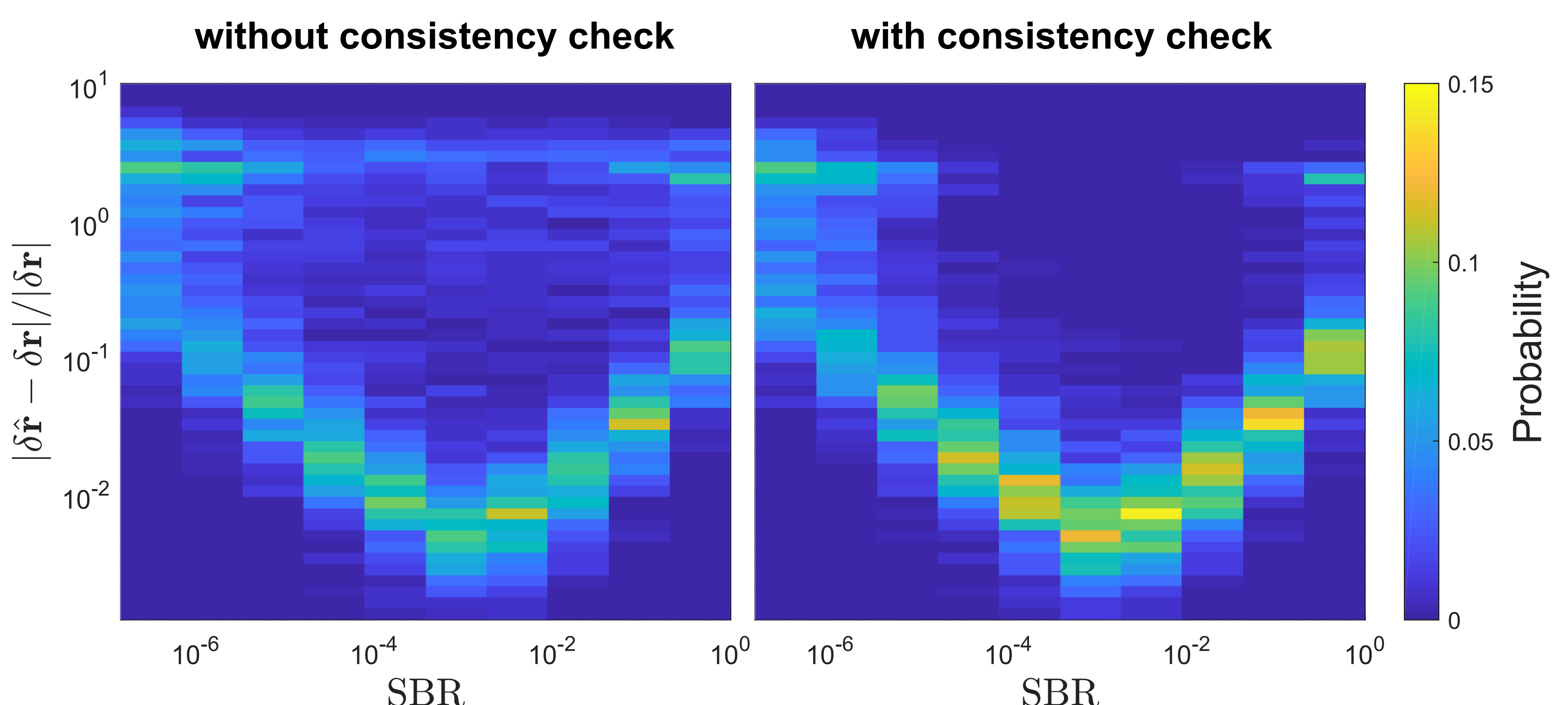
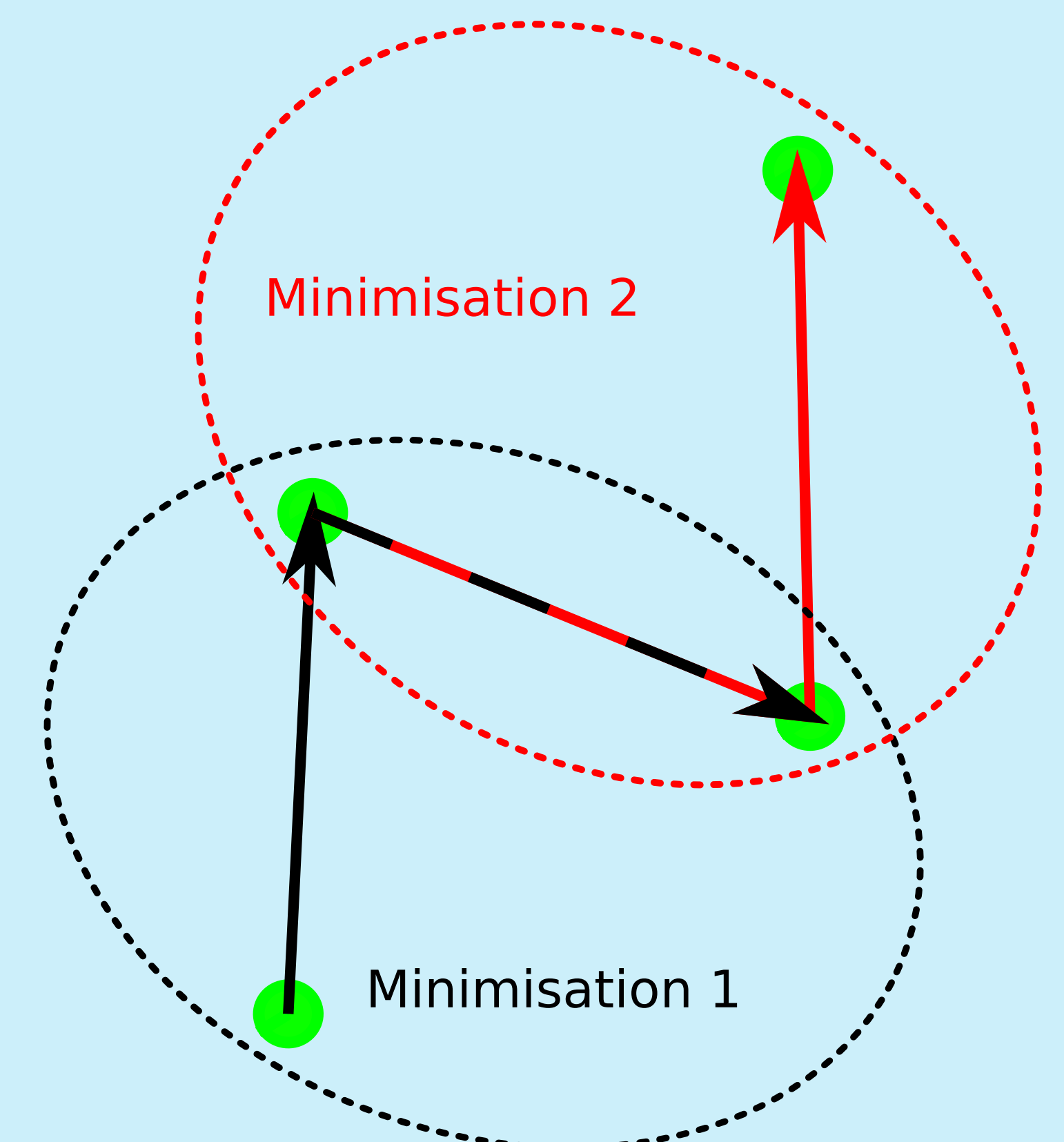
$$(\hat{r}_{12}, \hat{r}_{23}) = \arg \min_{(r_{12}, r_{23})} \sum_{j=1}^N \left( \frac{\mathbf{u}(\phi_j) \cdot \Delta(\phi_j)}{|\mathbf{u}(\phi_j)|} \right)^2$$

## Results

- ▶ **Results from simulations:** point scatterer undergoing random walk with 90nm step size
- ▶ **Error in step estimate depends on the fringe amplitude relative to:**
  - A) the background speckle intensity (signal to background ratio, SBR)
  - B) the shot noise level (differential signal to noise ratio, dSNR)
- ▶ **Two regimes where algorithm performs poorly:**
  - A)  $SBR \geq 1$ , directly scattered intensity no longer negligible relative to interference
  - B) low dSNR, noise levels comparable to fringe amplitude
- ▶ **Optimal working regime:** achieves errors of order 1%, corresponding to subnanometre precision

## Consistency Check

- ▶ **Global least squares minimisation:** may converge to local minimum
- ▶ **Require consistency of step estimates:** run minimisation procedure with new start points until consistent trajectory achieved
- ▶ **Potential sign ambiguity:** symmetry of system means exact opposite transverse steps give same phase shift
- ▶ **Flip transverse steps estimates if it improves consistency**



1. J. Homola, S. S. Yee, and G. Gauglitz, "Surface plasmon resonance sensors: review," Sensors Actuators B54, 3-15 (1999).

2. R. W. Taylor and V. Sandoghdar, "Interferometric Scattering Microscopy: Seeing Single Nanoparticles and Molecules via Rayleigh Scattering" Nano Lett.19, 4827-4835 (2019).

3. S. A. Maier, "Plasmonics: Fundamentals and Applications" (Springer, 2007), 1st ed.